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Author(s): Gonzales, Ivana

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Computational material design for energy and gas storage applications

Ivana Gonzales

Physics and Chemistry of Materials
Los Alamos National Laboratory (LANL)
Los Alamos, USA

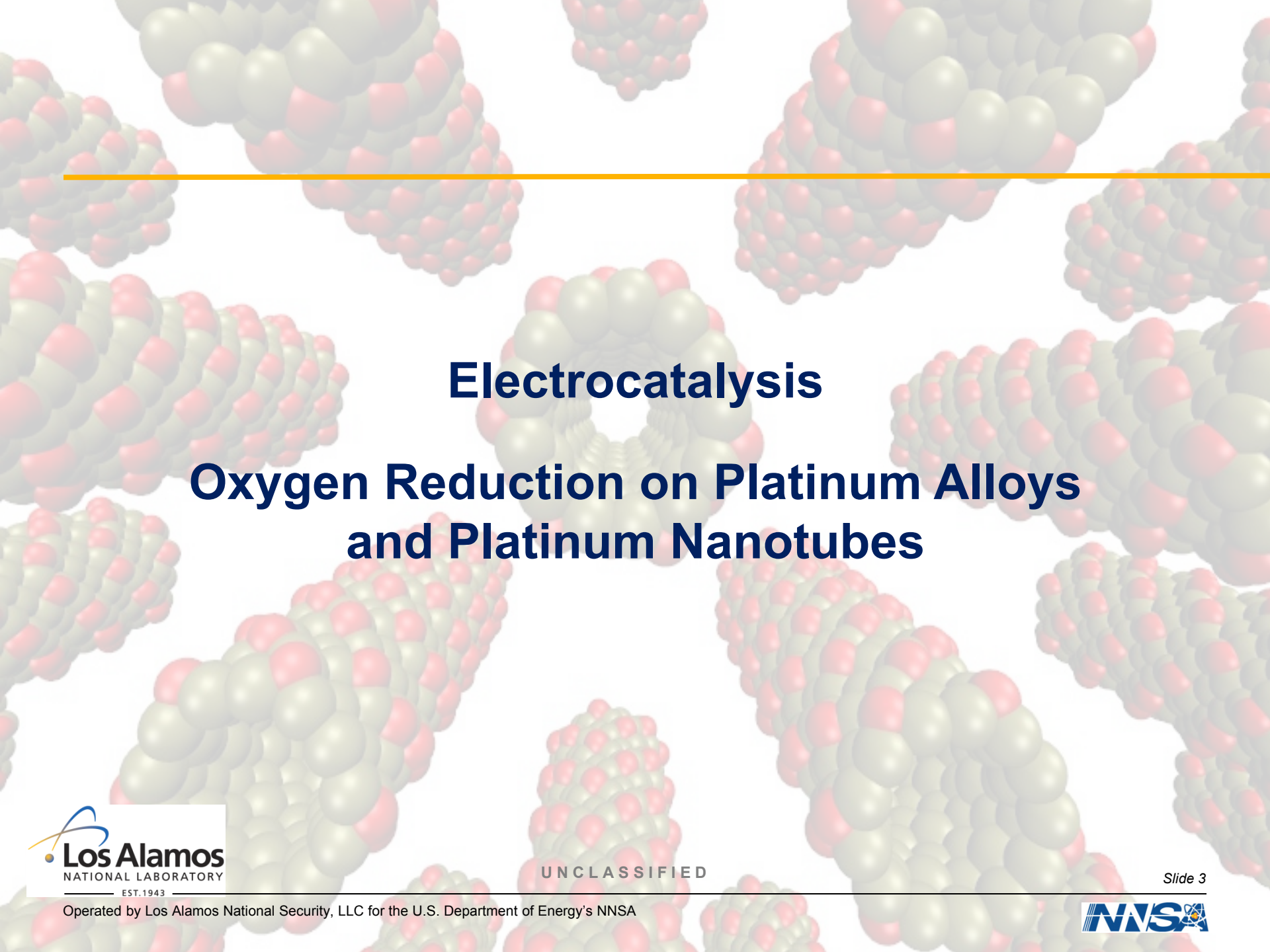
UNM, February 2013

Overview

Energy Storage in Chemical Bonds:

- Electrocatalytic reduction of oxygen on platinum alloys and nanostructures
- Electrocatalytic reduction of nitrogen on molybdenum nitride

Hydrogen Storage in Metal Organic Frameworks



Electrocatalysis

Oxygen Reduction on Platinum Alloys and Platinum Nanotubes

Introduction

Fuel cells have a potential for highly efficient use of chemical fuels, compared to heat engines

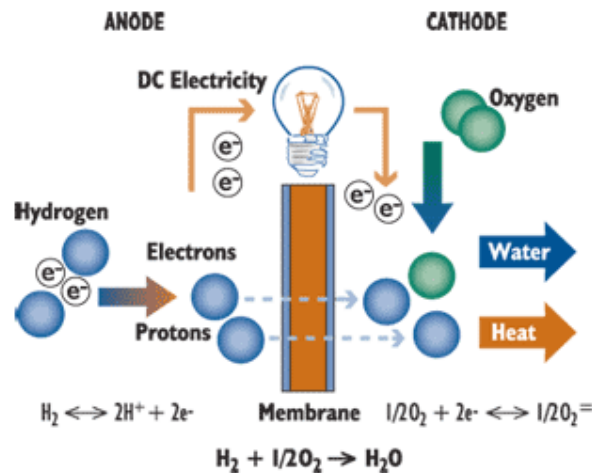
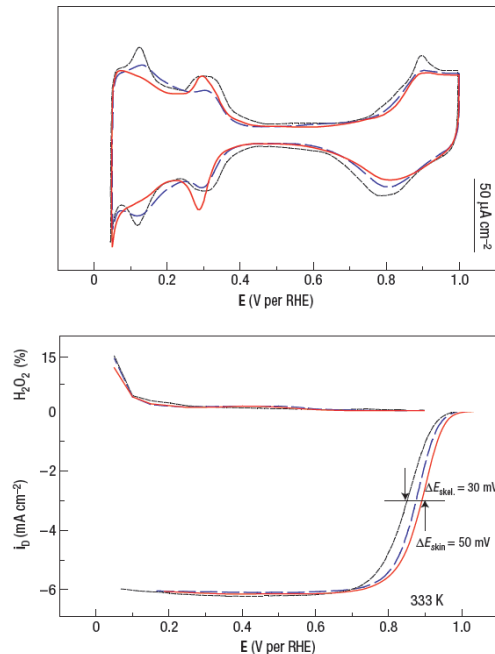


Figure: hydrogen/oxygen fuel cell

Introduction

slow kinetics of the oxygen reduction reaction (ORR) in acidic environment



significant cathode overpotential decreases the fuel cell electrical efficiency:

overpotential of 500-600 meV - efficiency of 45-55 %
compared to the theoretical thermodynamic efficiency of 93 %
at 25°C.

$$\Delta_r G_{\text{cell}} = -nF\Delta E_{\text{cell}}$$

Figure: Cyclic voltammograms and polarization curve of ORR on

Motivation

Reducing the ORR overpotential / cost:

(1) **alloying** platinum with platinum group metals

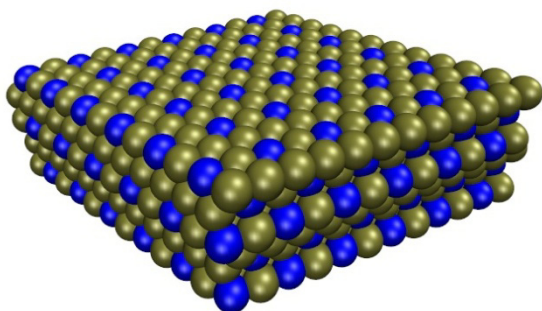


Figure: Pt₃Ni(111) surface

(2) **nanostructures**: nanotubes and nanoparticles

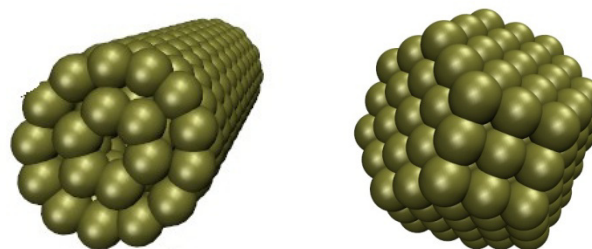
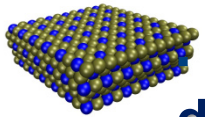
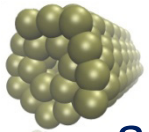


Figure: (6,6)@(13,13) MWPtNT nanotube and 2nm Pt₂₀₁ cluster

Motivation



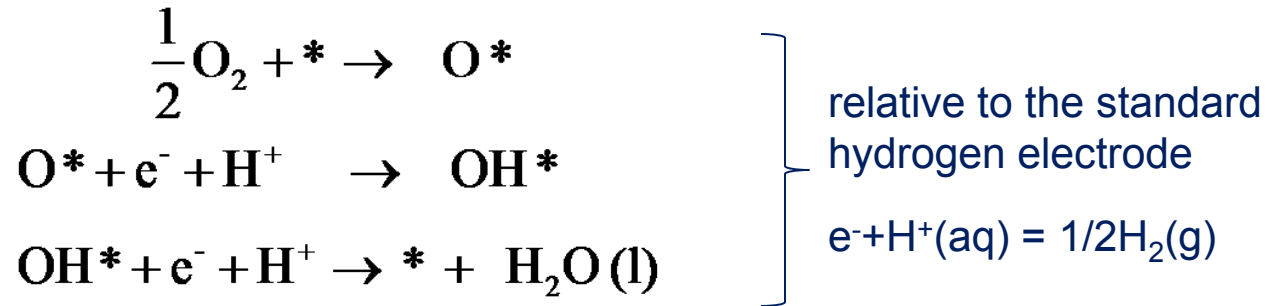
study the influence of alloying component **concentration and distribution** on the **ORR activity** and **stability** in aqueous environment



study the effect of **size and structure** of a nanomaterial on the ORR activity and stability in aqueous environment

Methodology - study of ORR mechanism

Reactions connecting different states of the metal surface(*) in the ORR mechanism

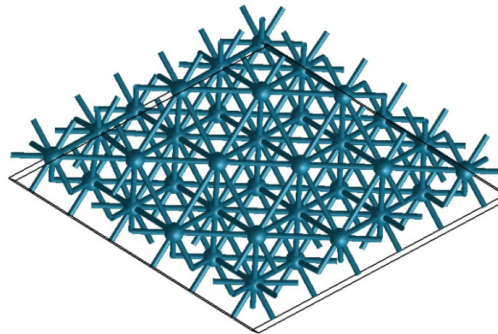


Free gibbs energy of the reactions

$$\begin{aligned}
 \Delta G_{\text{w,water}} &= \Delta E_{\text{w,water}} + \Delta \text{ZPE} + T\Delta S \\
 \Delta G(U, \text{pH}, T = 298\text{K}) &= \Delta G_{\text{w,water}} \underbrace{- eU}_{\text{bias effect}} + \underbrace{kT \ln(10) \text{pH}}_{\text{correction for the free energy of H}^+}
 \end{aligned}$$

Technical details

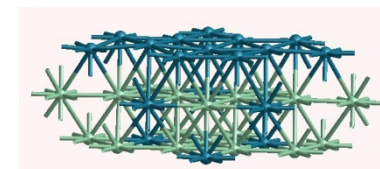
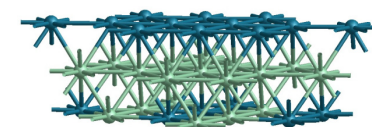
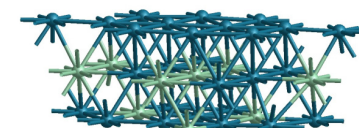
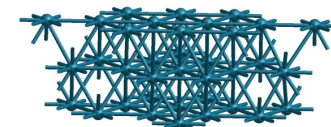
- VASP program
- DFT with PAW method using GGA approximation with PW91, PBE and RPBE exchange-correlation terms
- 3 layer $2\sqrt{3} \times 2\sqrt{3}$ (111) slab with 13.5 Å vacuum layer
- effect of solvent – bilayer of water molecules on the surface
- 4 x 4 x 1 k-point Monkhorst-Pack mesh
- plane-wave basis with a cutoff energy of 400 eV
- Methfessel-Paxton smearing of order 2 with sigma value of 0.2 eV



Oxygen Reduction Reaction: Energetics

Table: The binding Enthalpies and Free energy changes at U=0 V and pH=0 for different absorbents with water on Pt surfaces with different concentration of Ni in a second layer (1/3 coverage)

		OH* + e ⁻ + H ⁺	O* + 2(e ⁻ + H ⁺)	H* - e ⁻ + H ⁺
Pt(111)	$\Delta E_{w,water}$	0.45 eV	1.43 eV	-0.38 eV
	$\Delta G_{w,water}$	0.80 eV	1.48 eV	-0.14 eV
	U_f	0.8 V	0.74 V	0.14 V
Pt ₃ Ni(111)seg	$\Delta E_{w,water}$	0.74 eV	2.04 eV	-0.16 eV
	$\Delta G_{w,water}$	1.09 eV	2.09 eV	0.08 eV
	U_f	1.1 V	1.40 V	-0.08 V
PtNi(111)seg	$\Delta E_{w,water}$	0.97 eV	2.34 eV	-0.01 eV
	$\Delta G_{w,water}$	1.32 eV	2.39 eV	0.23 eV
	U_f	1.32 V	1.20 V	-0.23 V
PtNi ₃ (111) seg	$\Delta E_{w,water}$	1.05 eV	2.43 eV	0.10 eV
	$\Delta G_{w,water}$	1.40 eV	2.48 eV	0.34 eV
	U_f	1.4 V	1.24 V	-0.34 V



Oxygen Reduction Reaction: Free energy diagrams

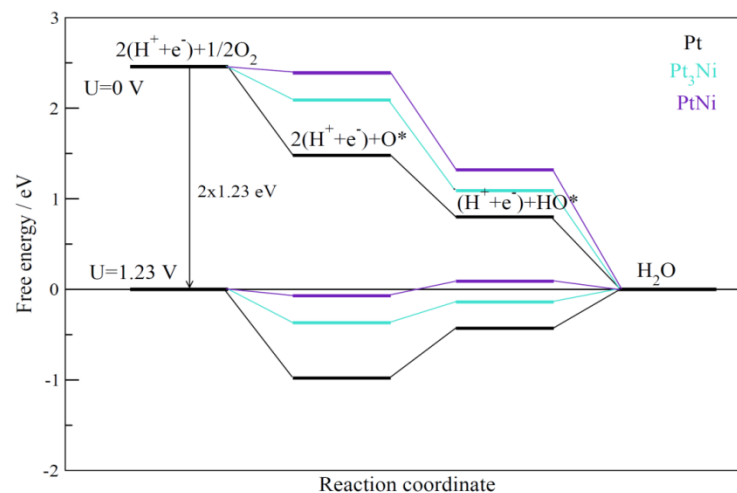
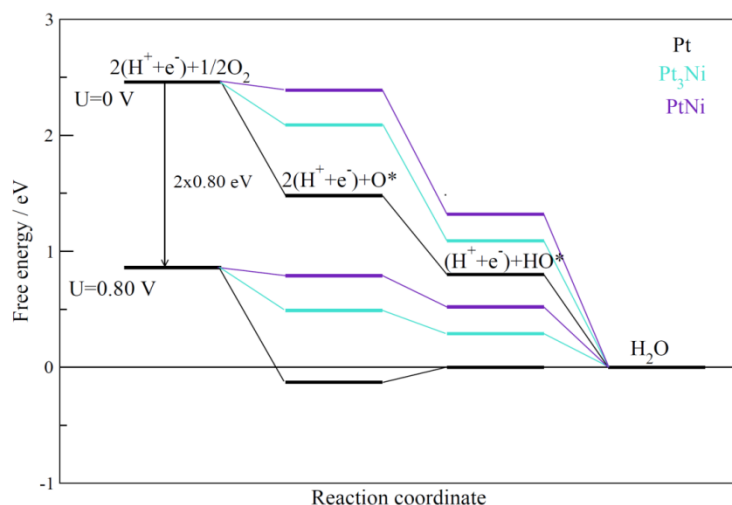
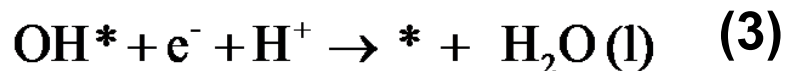
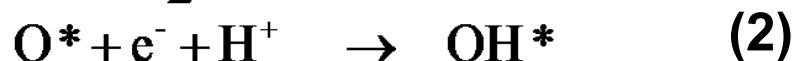
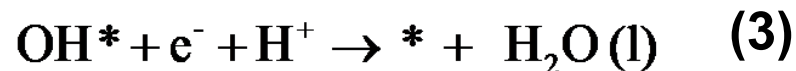
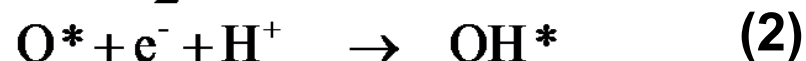


Figure: Free-energy diagrams for ORR over Pt(111) surfaces with different Ni concentration in the second layer, for cell potentials $U=0.80 \text{ V}$ and $U=1.23 \text{ V}$

Oxygen Reduction Reaction: Free energy diagrams



estimated catalytic activity:



$$550 > 240 > 190 > 150 \text{ mV}$$

confirmed experimentally:

Y. Liu et al, J. Phys. Chem. C, 116, 7848 (2012)

M. Karpenter, JACS, 134, 8535 (2012)

Stability of the surfaces

Estimate of the shift in the electrochemical dissolution potential

Table: surface cohesive energy and the estimate of the shift in the electrochemical dissolution potential relative to Pt(111)

reaction	$M_N(\text{surface}) \rightarrow M_{N-1} + M$	$\Delta E/\text{eV}$	$\Delta U_{\text{corr}}/\text{V}$	$\Delta U_{\text{corr}}^b/\text{V}$
Pt(111)		5.79	0.00	0.00
Pt ₃ Ni(111)	site 1	6.11		
	site 2	6.23		
	site 3	6.04	+0.13	+0.10
PtNi(111)	site 1	6.41		
	site 2	6.38	+0.30	+0.30
PtNi ₃ (111)	site 1	5.69		
	site 2	5.58	-0.11	-0.23

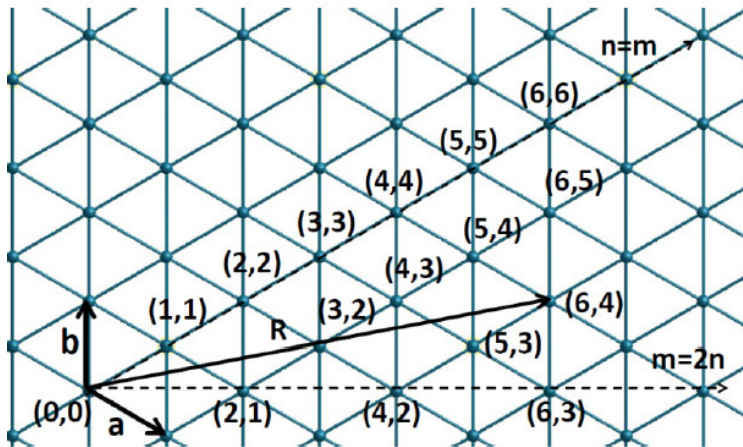
PtNi₃

- more susceptible to electrochemical dissolution of Pt monolayer
- more susceptible to poisoning of the surface by the formation of nickel oxide

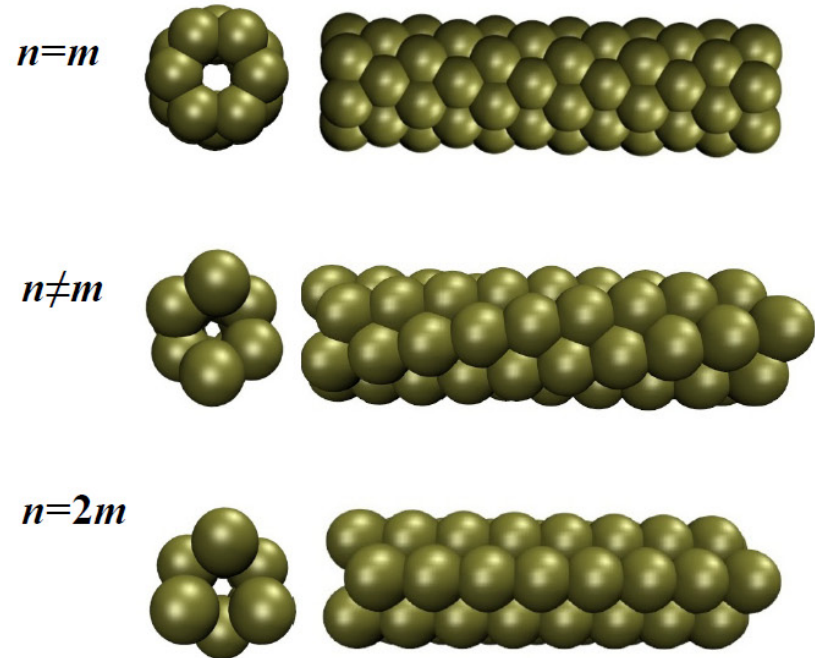
I. Matanovic et al. J. Phys. Chem. C, 115, 10640 (2011)

Pt nanotubes

PtNT: Rolling-up Pt(111) sheet to form a tube



Roll-up
→

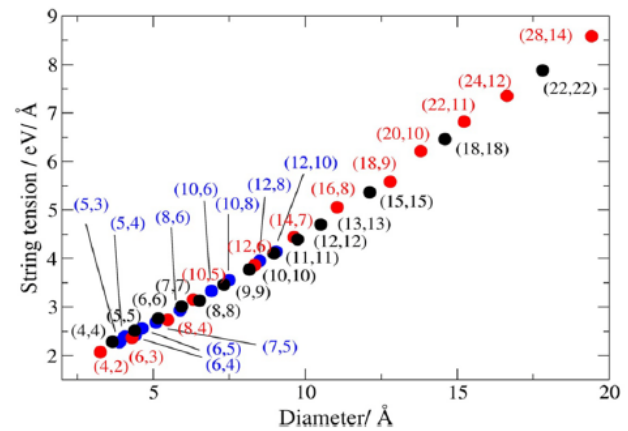
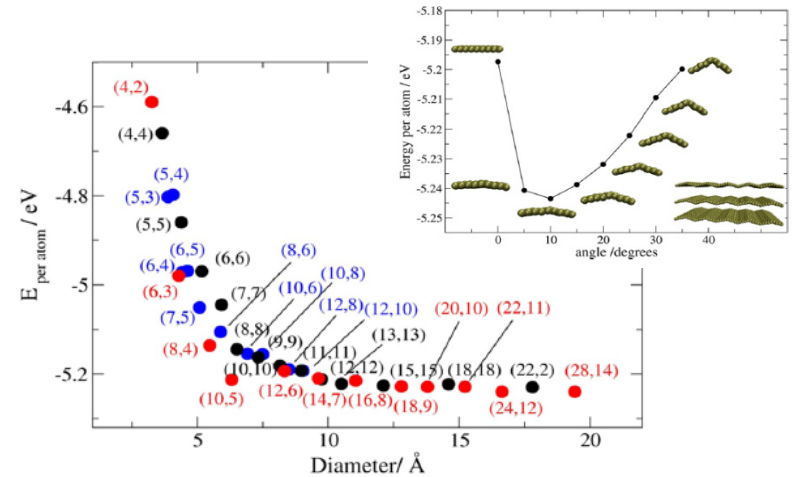
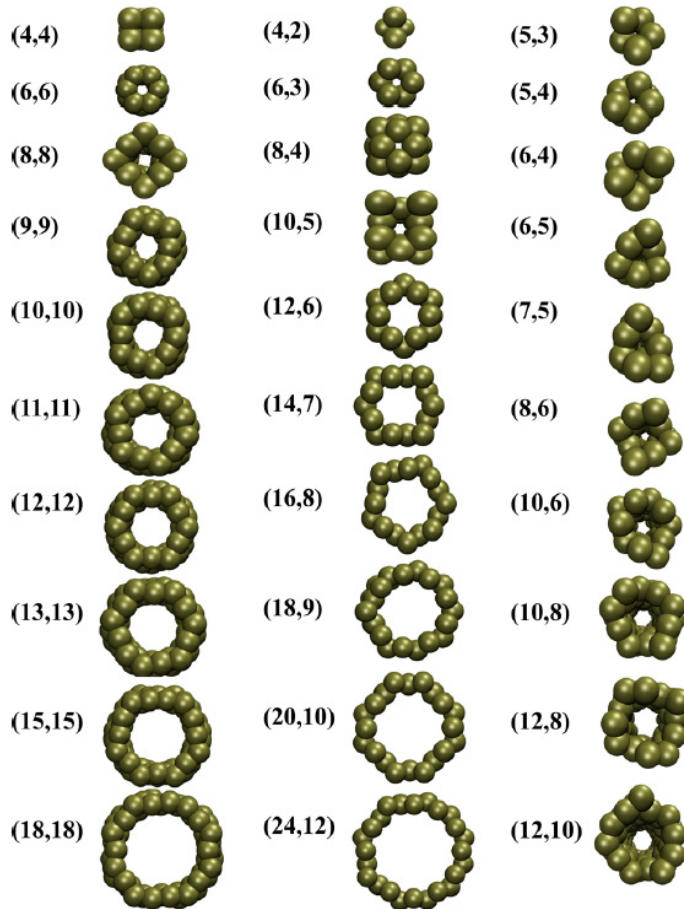


rolling vector: $R = na + mb$

$$r = \frac{\sqrt{2}a_c}{4\pi} \sqrt{n^2 + m^2 - nm}$$

$$a_c = 3.70 - 3.85 \text{ \AA}$$

Pt nanotubes



Pourbaix diagrams

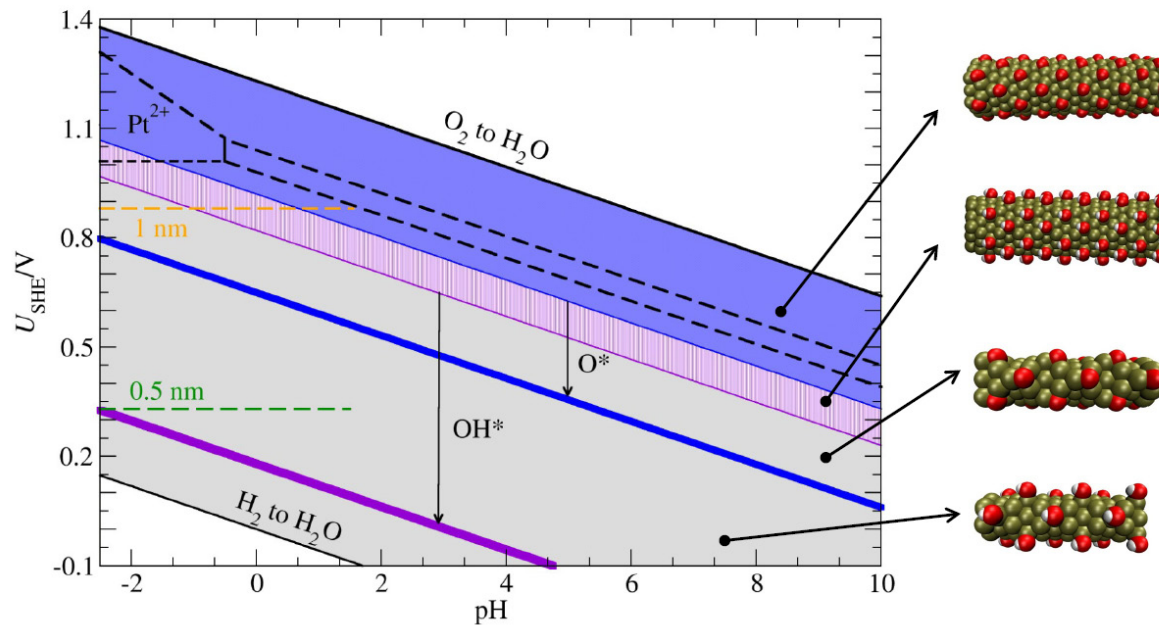


Figure: Calculated surface Pourbaix diagrams for Pt nanotubes compared to a bulk Pourbaix diagrams (black dashed lines)

Dissociative oxygen reduction reaction (ORR) mechanism

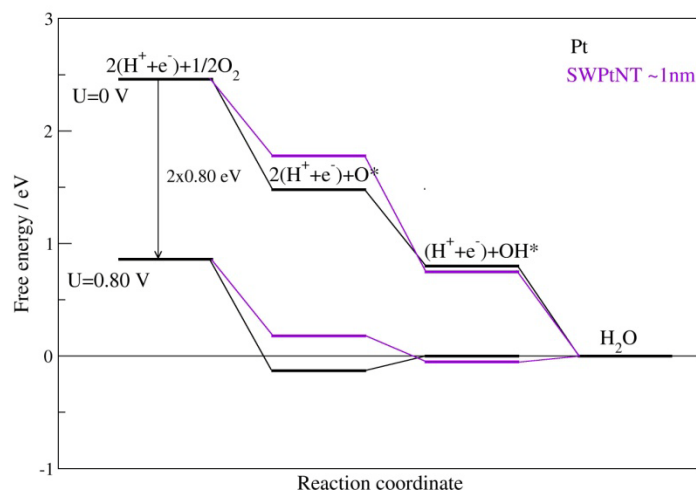
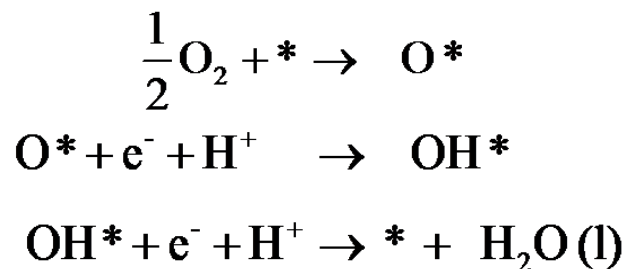


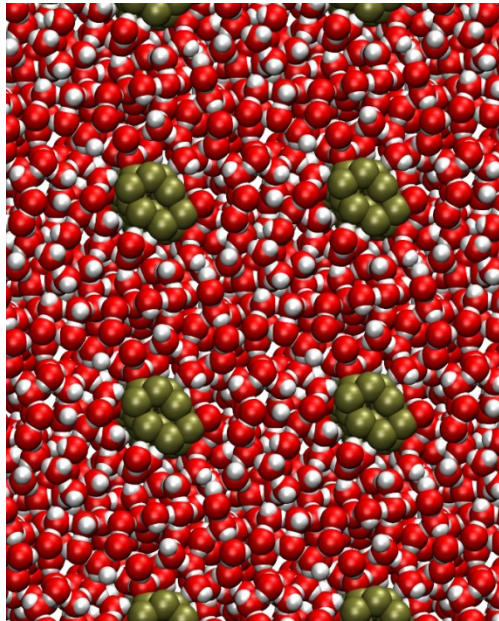
Figure: Free-energy diagrams for ORR over Pt(111) surfaces and SWPtNT for cell potentials U=0.80 V

PtNTs, d ~ 1nm
smaller ORR overpotential than
Pt(111), up to 100 meV

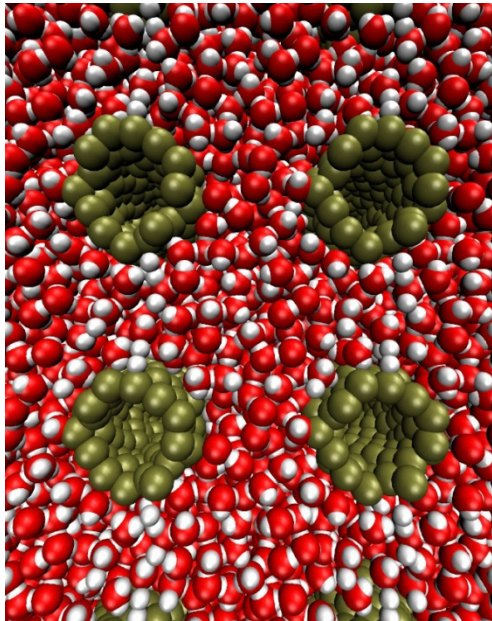
Pt nanotubes – ab initio MD simulations in water

- Aim** (1) characterize change of atomic and electronic structure on solvation
(2) structure of water around curved surfaces - water-surface interface models

(6,6) and



(13,13) SWPtNT in water



~800 atom cell, 1300 MD steps
in 24h, 480 processors, average
~1min/step

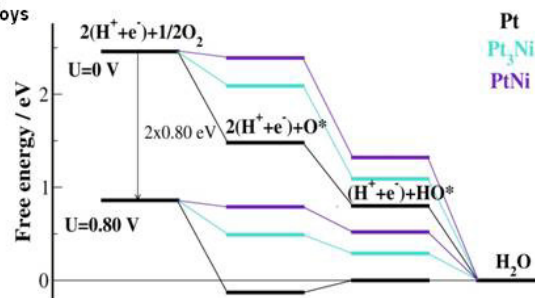
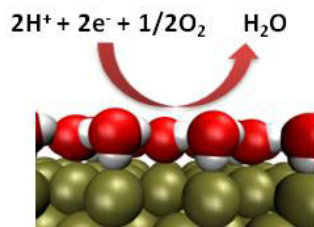
Conclusions

- catalytic activity – modification in the electronic structure induced by the specific subsurface composition

The ORR overpotential was found to decrease :



Oxygen reduction reaction on Pt-Ni alloys



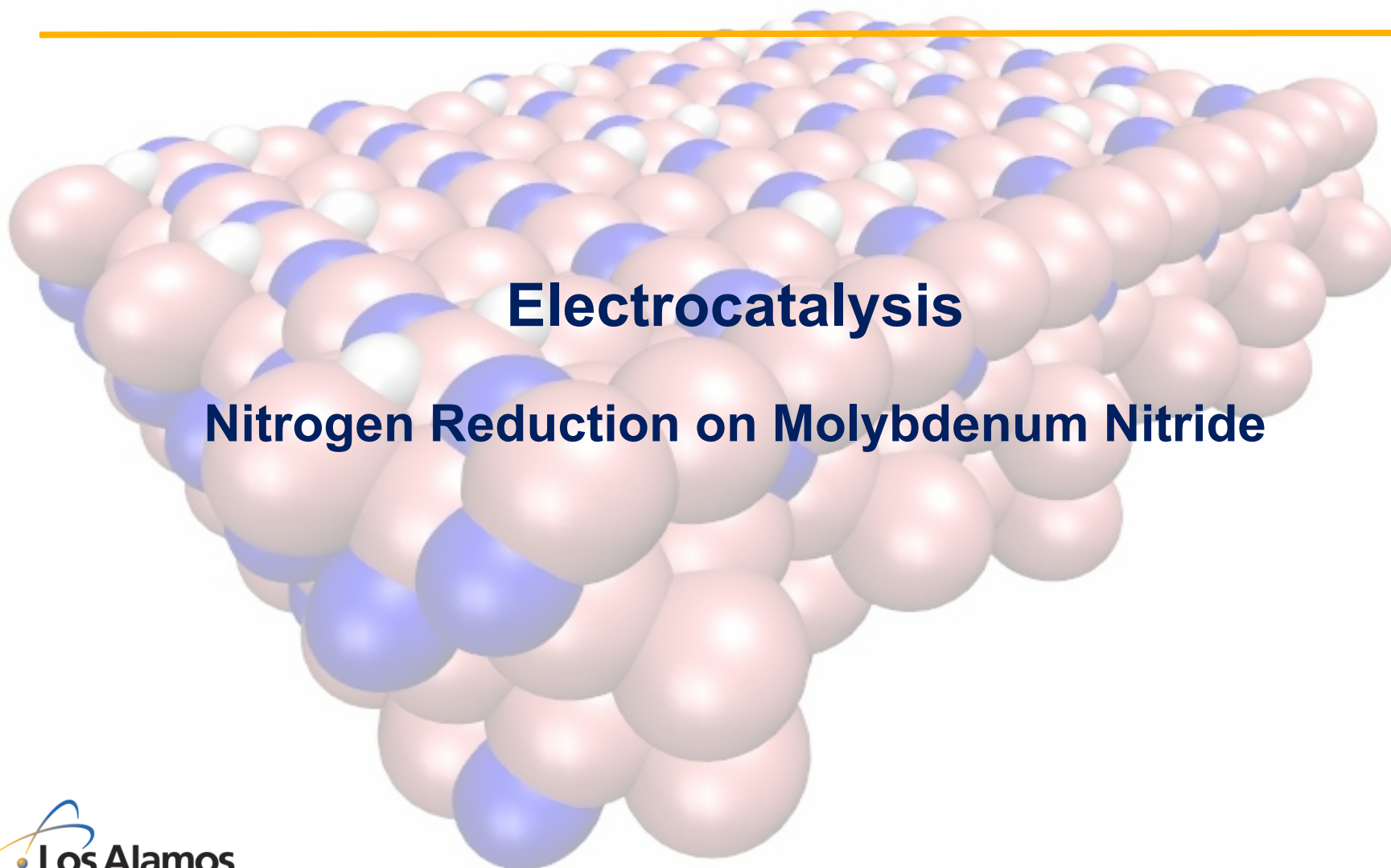
- shifts in the electrochemical dissolution potentials relative to Pt indicate that PtNi is the least susceptible to corrosion

Conclusions

- ~0.5 nm nanotubes bind oxygen/hydroxyl more strongly than Pt(111)
- ~1 nm nanotubes bind oxygen/hydroxyl comparable or weaker than Pt(111)
- reduced ORR overpotential – SWPtNT with a diameter > 1nm
- control size/chirality – fine tuning of reactivity → separation of metal nanotubes by geometric specification or size
- all studied nanotubes more susceptible to electrochemical dissolution than Pt(111) – potential corrosion problem

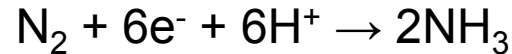
I. Matanovic et al. J. Phys. Chem. C, 116, 16499 (2012)

I. Matanovic et al, J. Electrochem. Soc, submitted



Electro-reduction of nitrogen

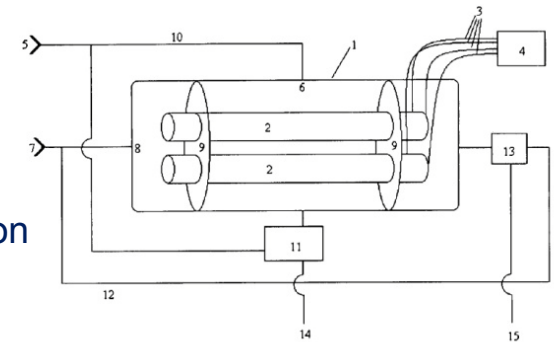
- ammonia can be obtained by electro-reduction of nitrogen



protons are supplied from electro-oxidation of hydrogen or water

Marnellos et al. Science 282 (5386) 98-100

Holbrook and Ganley, US patent 7811442 (2010):
electrochemical synthesis of ammonia using high temperature proton
conductors at atmospheric pressures



- challenges: development, characterization and optimization of **new electrocatalysts** for ammonia electrosynthesis and stable anhydrous **proton conducting electrolytes**

Introduction

- early transition metal nitrides - possible replacements for platinum-group metal catalysts
- demonstrated catalytic activity for isomerisation, dehydrogenation, hydrogenation, water gas shift and amination reactions with competitive rates

Mo_2N – high surface area films synthesized at LANL (polymer assisted deposition)

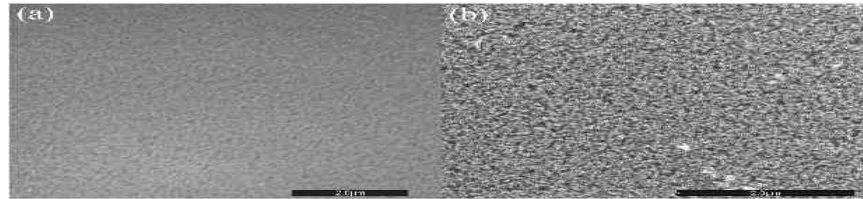
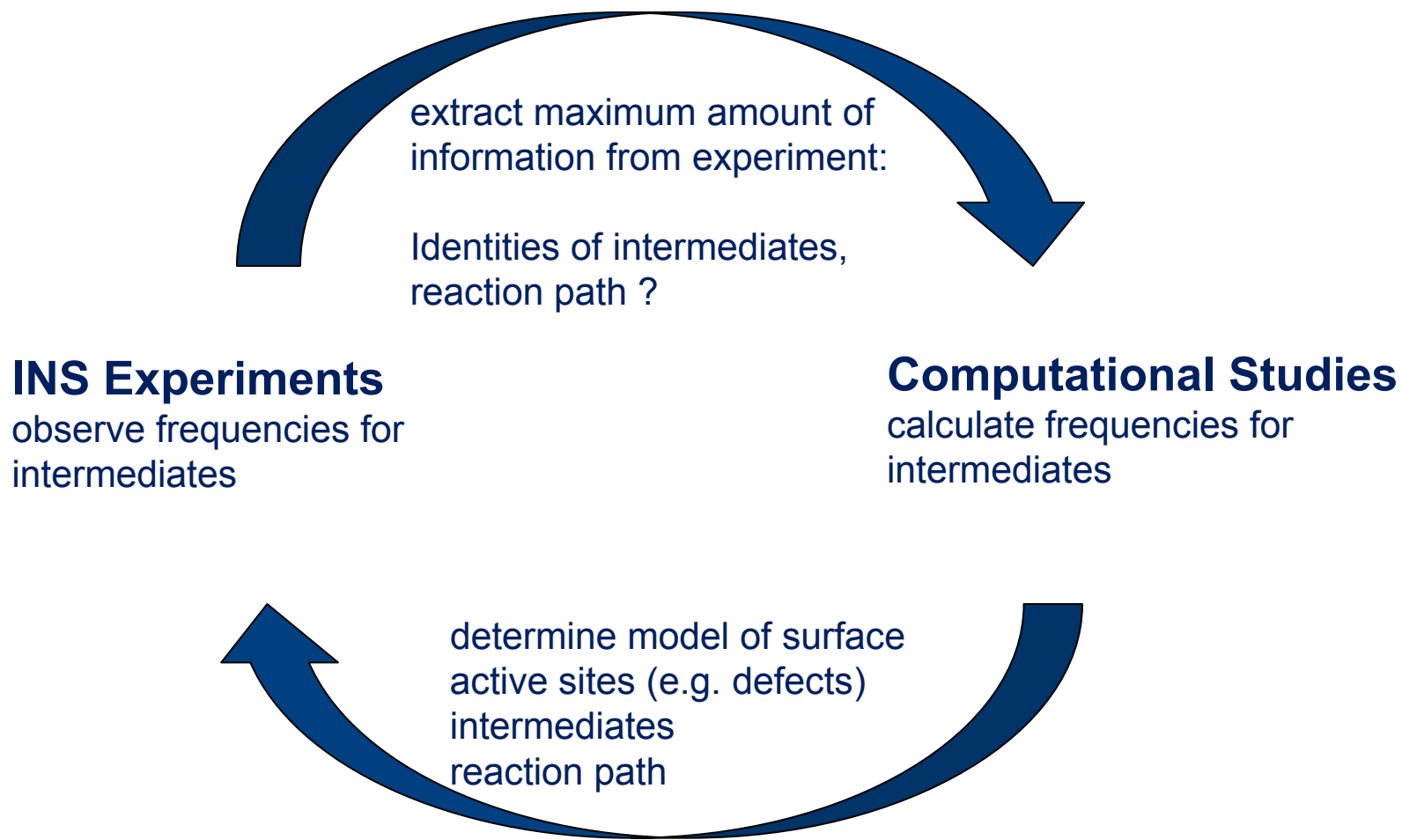


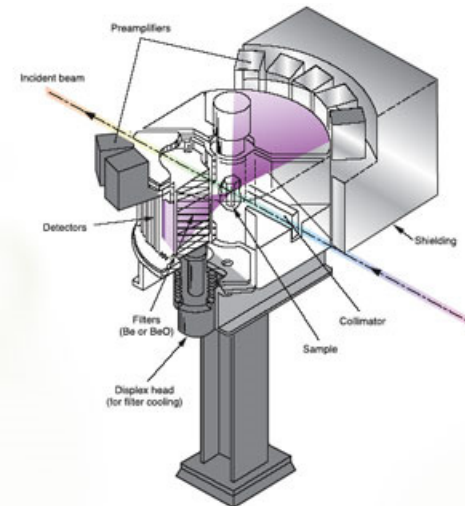
Figure: Field emission scanning electron microscope (FESEM) images

Synergy of Inelastic Neutron Scattering and Computation: Ammonia synthesis on novel material



Inelastic neutron scattering experiment

The Filter Difference Spectrometer (FDS) at LANL



- used for molecular vibrational spectroscopy by **inelastic neutron scattering**
- most useful for measurements requiring high sensitivity; for example, very dilute systems or molecules adsorbed on surfaces such as in catalysts

vibrational spectra measured on FDS

- < 1g sample of catalyst adsorb in-situ H_2 , then add N_2
- heat stepwise to increasing T
- collect INS spectrum at each step

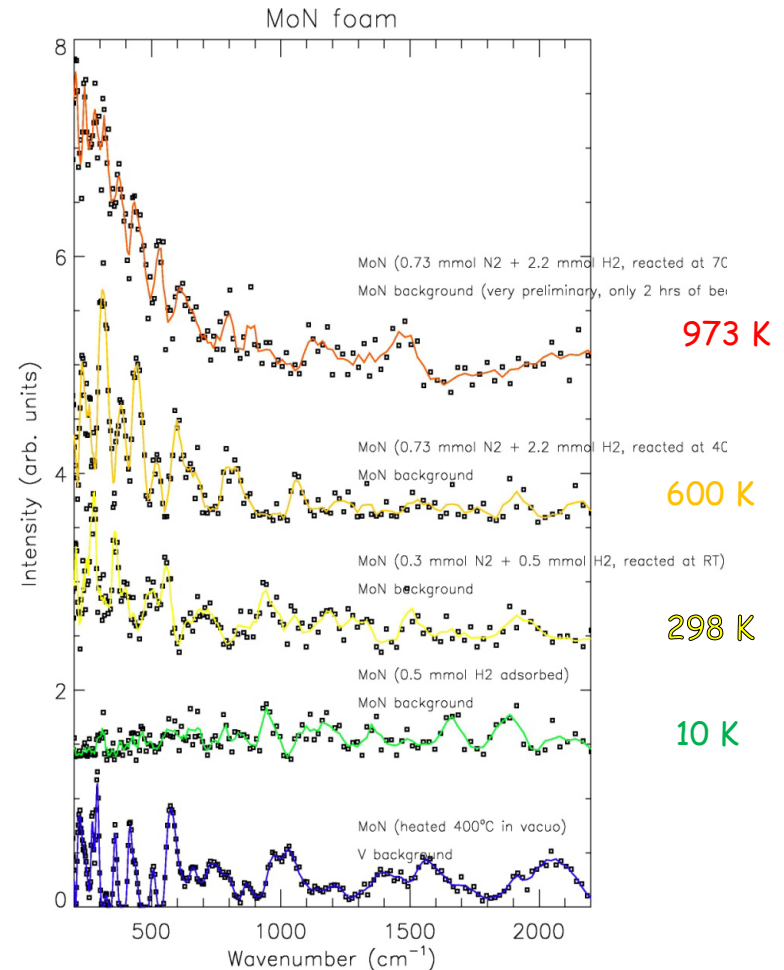
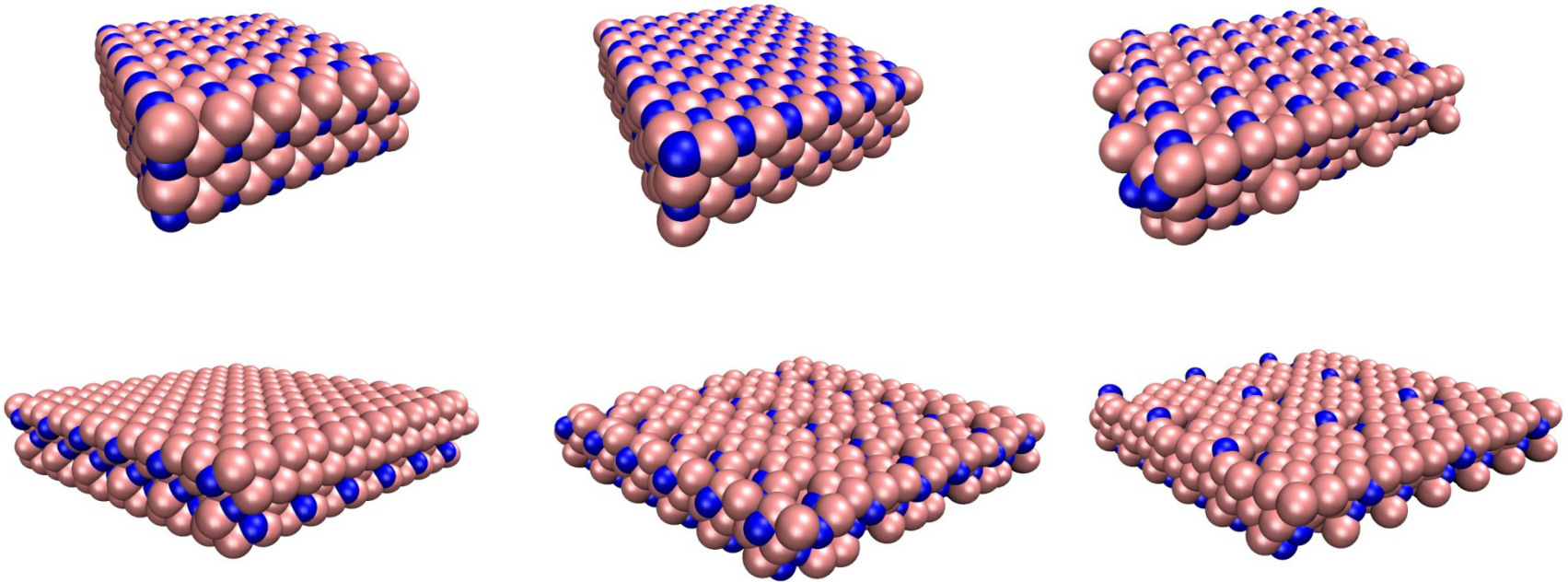


Figure: INS spectra of reactive species on MoN

Slide 26

Ammonia synthesis on novel MoN material

- model the surface
- model the reaction on the surface – identify the intermediates
- model the INS spectra – compare with the experiment



reactivity of γ -Mo₂N towards hydrogen

	(001)/eV	(100/010)/eV	(111)/eV	(111)*	(101)/eV
$\Delta E(\text{H}_2)$	does not bind	-0.46	-0.81	dissociates	dissociates
$\Delta E(\text{H})$ terminal1	-2.34	-2.53			
$\Delta E(\text{H})$ terminal2		-2.40			
$\Delta E(\text{H})$ bridging	-2.03	-2.69		-3.28	-3.80
$\Delta E(\text{H})$ fcc			-3.48	-3.22	

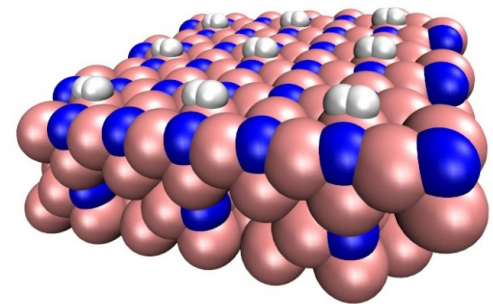
* surface with defects introduced

different surfaces – very different reactivity: (001) does NOT adsorb H₂, (101) and (111) + defects dissociates H₂

molecular chemisorption (Kubas dihydrogen complex)

$d(\text{Mo}-\text{H}_2) = 1.86 \text{ \AA}$

$d(\text{H}-\text{H}) = 0.85 \text{ \AA}$ (activated H-H bond)



reactivity of γ -Mo₂N towards hydrogen

	(001)/cm ⁻¹	(100/010)/cm ⁻¹	(111)/cm ⁻¹	(111)* /cm ⁻¹	(101)/cm ⁻¹
H terminal1	1745, 739	1732, 727			
H terminal2	n/a	1675, 731			
H bridging	1208, 910	829, 701		1280, 1157	1339, 1231
H fcc			1233, 951, 823	1260, 1013	

- intensities calculated from DFT vibrational frequencies ω_k and amplitudes C^k

double differential cross section

$$\frac{d^2\sigma}{d\Omega dE} = \frac{\mathbf{k}}{\mathbf{k}_0} \sum_i \frac{\sigma_i^{\text{inc}}}{4\pi} S_i^{\text{inc}}(\mathbf{Q}, \omega)$$

incoherent cross section for atom i

$$S_i^{\text{inc}}(\mathbf{Q}, \omega) = \exp(-Q^2 \langle \mathbf{u}_i^2 \rangle) \frac{\hbar |Q \cdot C_i^k|}{2\omega_k} \delta(\omega - \omega_k)$$

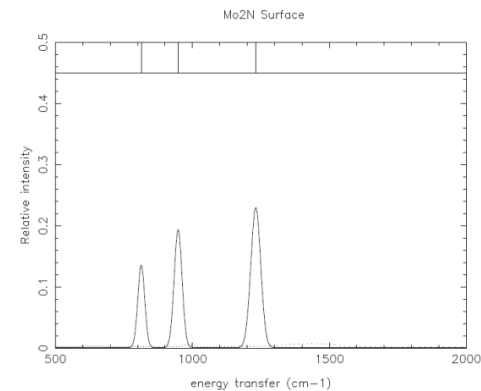
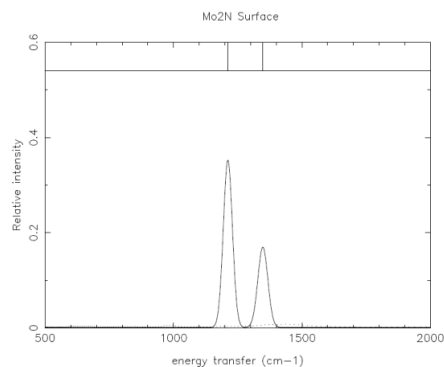
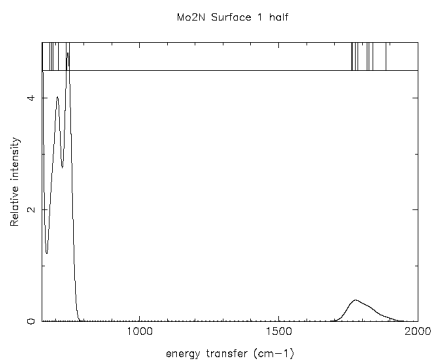
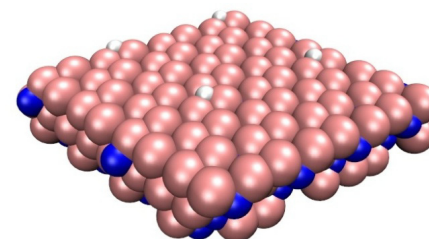
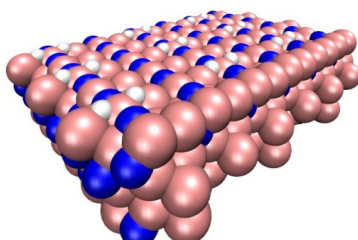
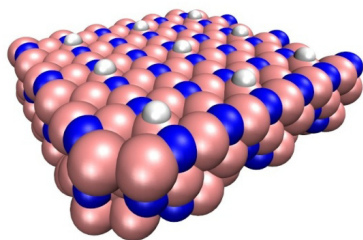
momentum transfer

experimental value: $\mathbf{Q} = \mathbf{k} - \mathbf{k}_0$

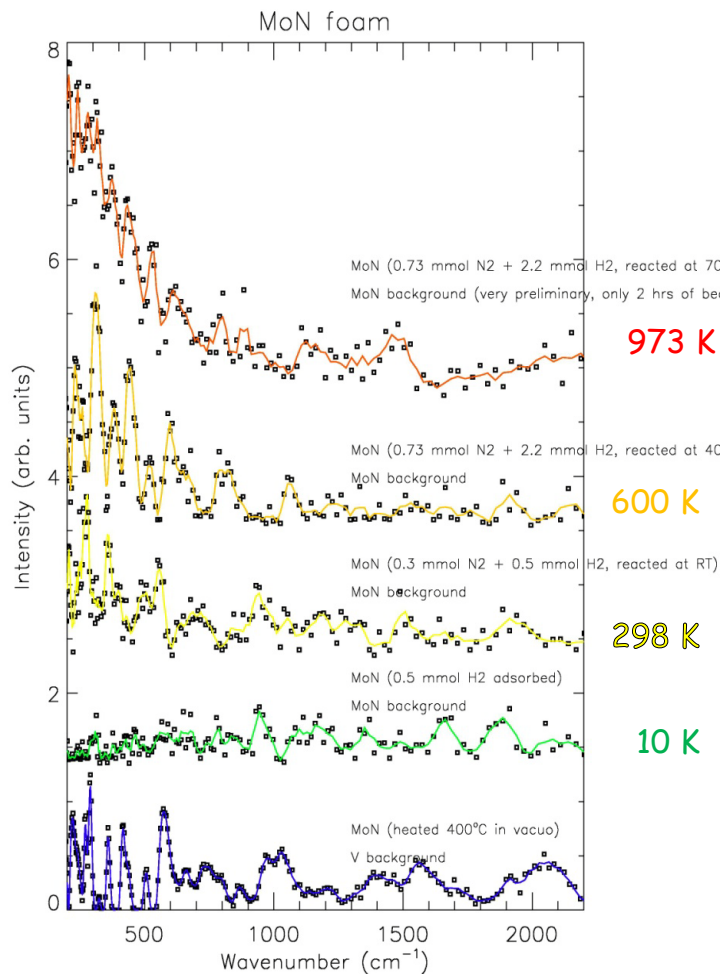
mean-square amplitude for atom i

reactivity of γ -Mo₂N towards hydrogen

	(001)/cm ⁻¹	(100/010)/cm ⁻¹	(111)/cm ⁻¹	(111) [*] /cm ⁻¹	(101)/cm ⁻¹
H terminal1	1745, 739	1732, 727			
H terminal2	n/a	1675, 731			
H bridging	1208, 910	829, 701		1280, 1157	1339, 1231
H fcc			1233, 951, 823	1260, 1013	



INS spectra assignment



(10 K) fcc H: 950, 1250 cm⁻¹
bridging H: ~ 600, ~800, 1140 cm⁻¹
terminal H: ~700, 1645 cm⁻¹

Figure: INS spectra of reactive species on MoN

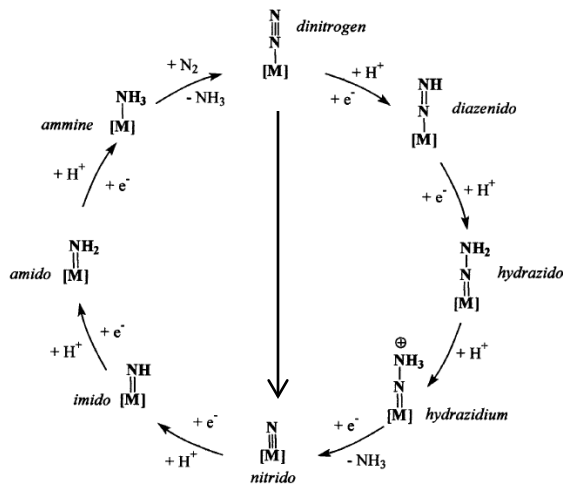
UNCLASSIFIED

Slide 31

reactivity of γ -Mo₂N: adsorption energies

- DFT calculations used to estimate the free energy of each elementary step in ammonia synthesis

$$\Delta G = \Delta E + \Delta E_{\text{ZPE}} + T\Delta S$$

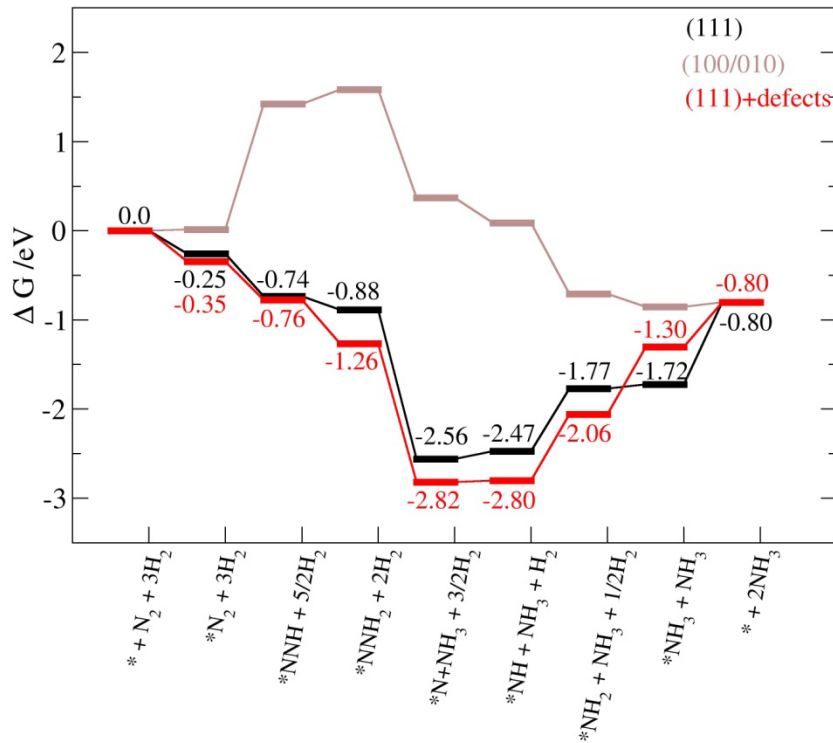


	$\Delta E_{(100/010)}/\text{eV}$	$\Delta E_{(111)}/\text{eV}$	$\Delta E_{(111*)}/\text{eV}$
N ₂	-0.65	-0.92	-1.01
N	-4.88	-7.84	-8.07
NNH	-1.65	-2.42	-2.51
NNH ₂	-2.94	-4.15	-4.34
NNH ₃	-2.41	-4.17	-5.64
NH	-3.86	-6.42	-6.75
NH ₂	-2.97	-4.03	-4.32
NH ₃	-0.95	-1.82	-1.40

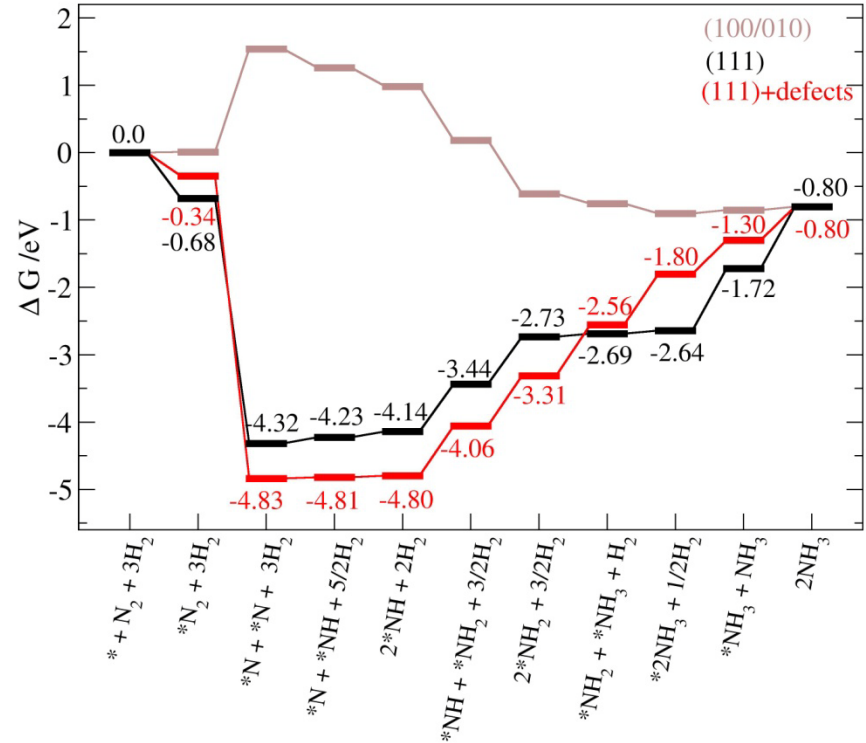
* surface with defects introduced

reactivity of $\gamma\text{-Mo}_2\text{N}$: energetics

associative mechanism

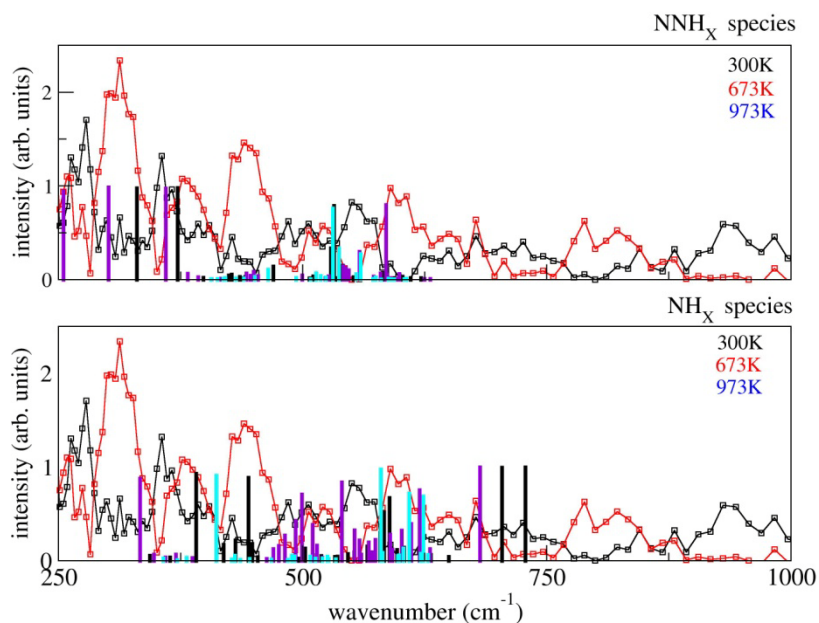


dissociative mechanism

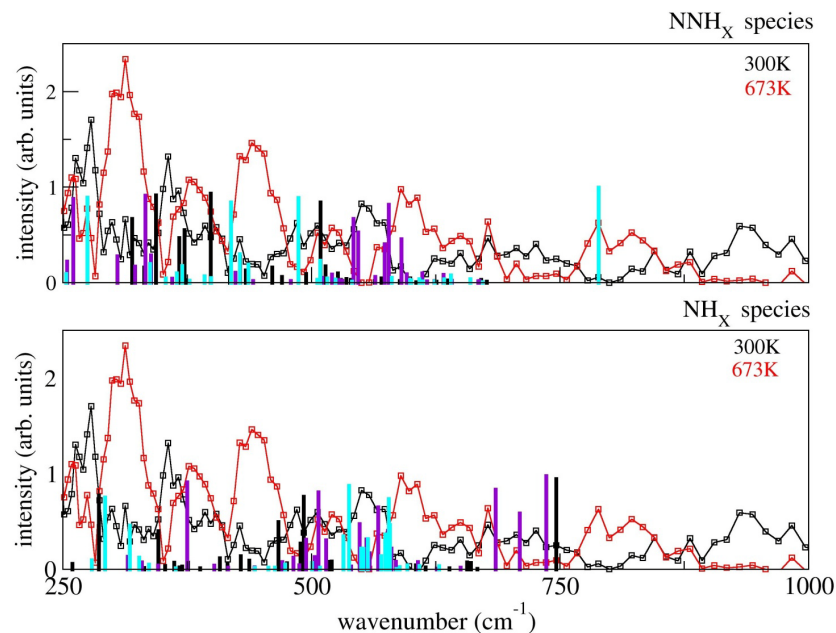


INS spectra: (111) perfect surface

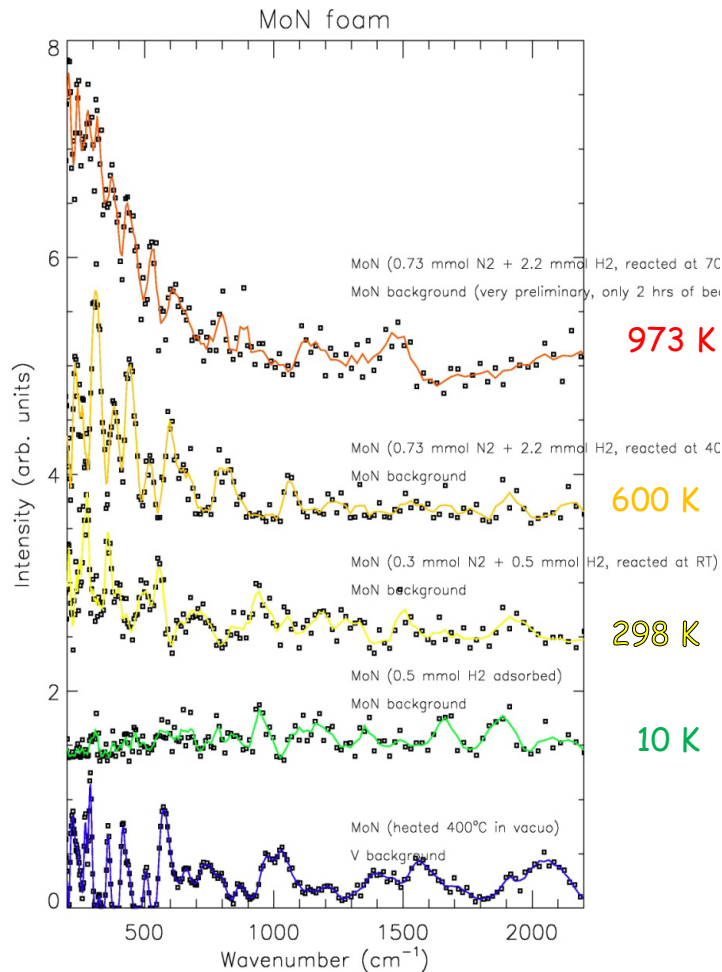
(111) perfect surface



(111) surface with defects



assignment



(973 K) NNH_x species gone; mainly NH_x species left.
ammonia phonon DOS states below 400 cm⁻¹
Mo-(NH₃) complex, incl. (NH₃) torsion at 120 cm⁻¹ !!
Peaks at ~ 600, 800, 900, 1150 and 1475 cm⁻¹

(600 K) H species gone; peaks at 425, 510, 600, 660, 725, 1070, (weak: 1240, 1550), 1900 cm⁻¹:
mainly NNH and NNH₂;
plus more strong peaks below 400 cm⁻¹:

(298 K) Similar to (10 K), but fewer H species,
new peaks at ~500, 700 and 1550cm⁻¹: NNH

(10 K) fcc H: 950, 1250 cm⁻¹
bridging H: ~ 600, ~800, 1140 cm⁻¹
terminal H: ~700, 1645 cm⁻¹

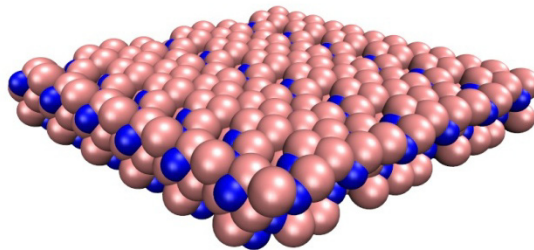
Figure: INS spectra of reactive species on MoN

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Slide 35

Conclusions

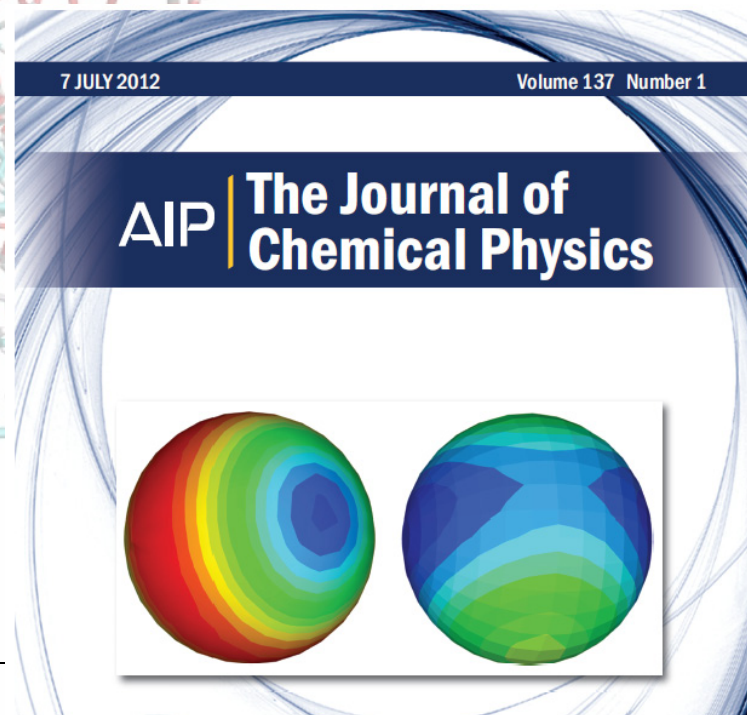
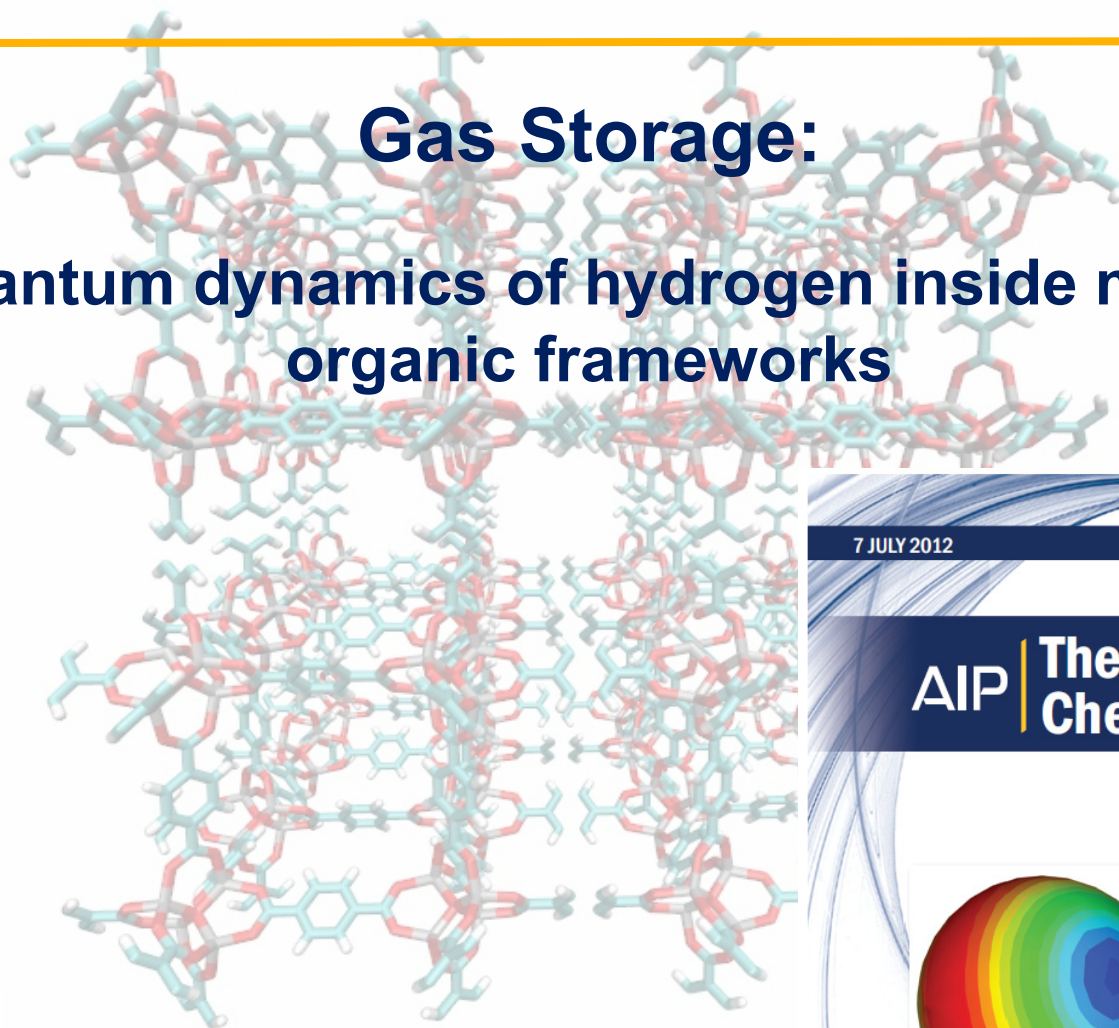
- we have investigated the catalytic mechanism and the active sites of newly synthesized material using inelastic scattering of neutrons and DFT calculations
- different surfaces have very different reactivity towards N_2 , H_2 and NNH_x , NH_x species
- active sites: (111) defect sites with under-coordinated Mo



- synthesis of ammonia proceeds through the formation of both NNH_x and NH_x species

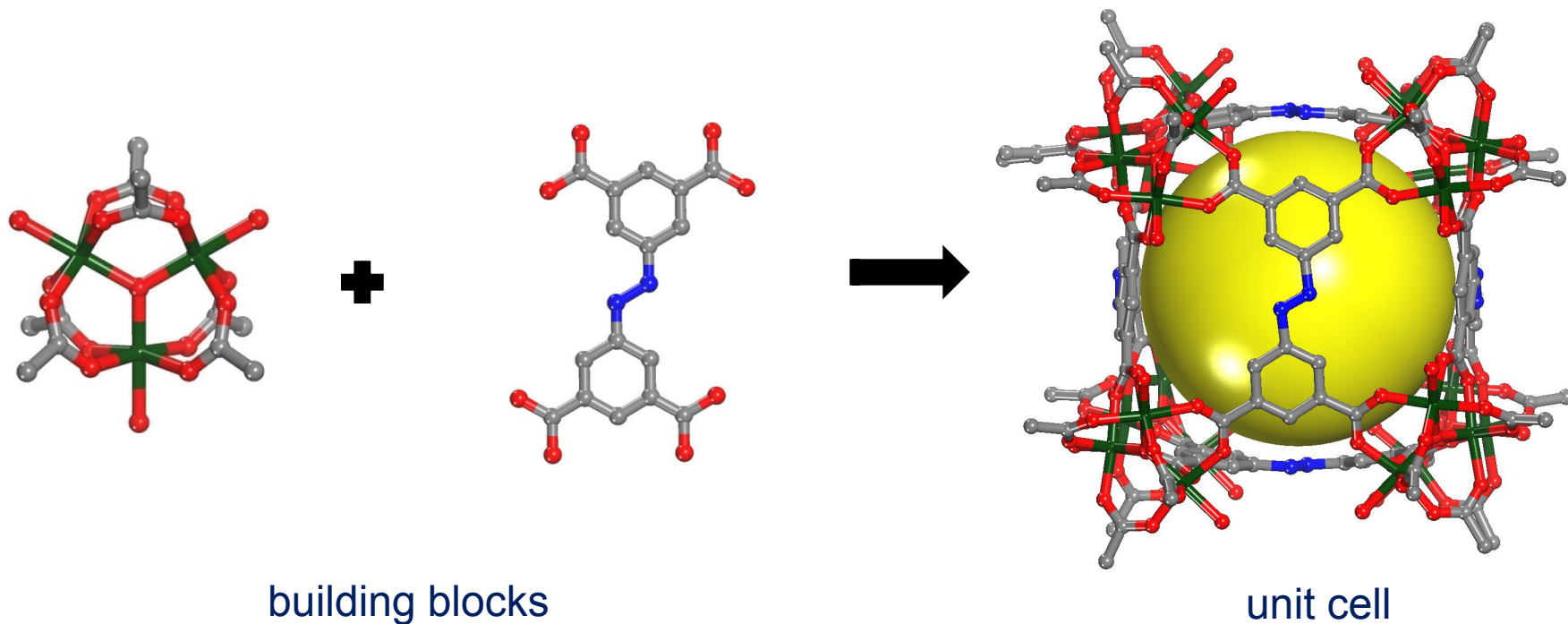
Gas Storage:

Quantum dynamics of hydrogen inside metal-organic frameworks



Introduction

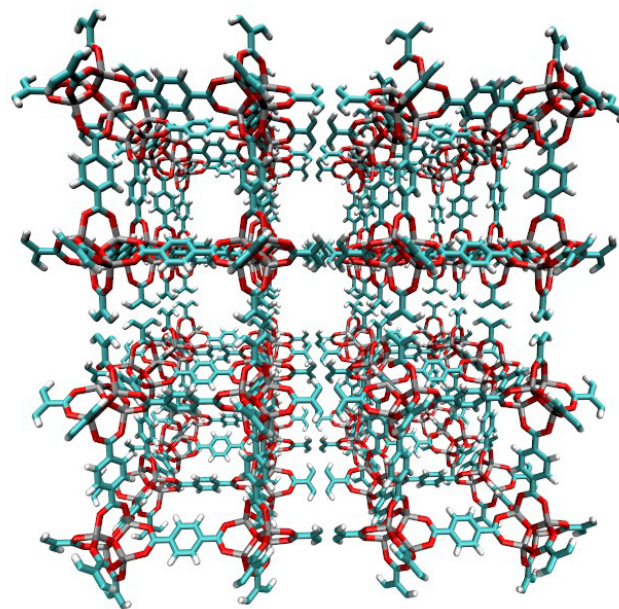
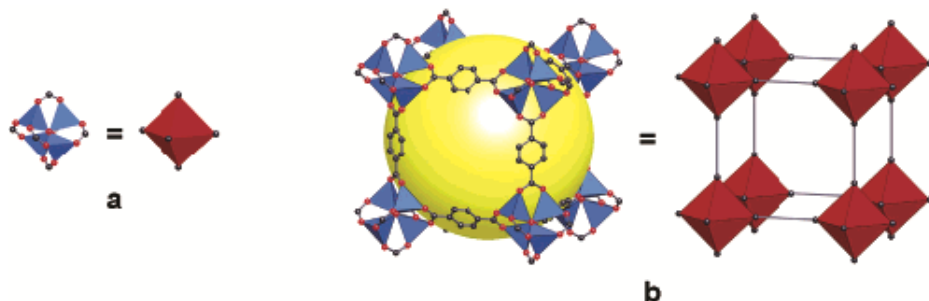
Metal organic frameworks (MOFs) - inorganic units connected with organic linkers



Introduction

applications: gas storage and separation (H_2 , CH_4 , CO_2), catalysis

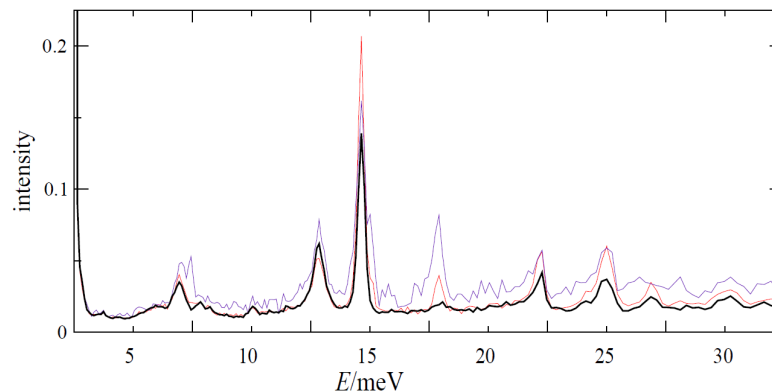
MOF -5 - close to the U.S. DOE requirements for on board hydrogen storage
7.1 wt % but at 40 bar and 77K



Motivation

understanding the INS spectra of H₂ in MOF-5

- wealth of information about excitations of translational and rotational motion of hydrogen - interactions of the guest molecule with the host



provide valuable insights in exploring the properties of these systems **at the molecular level** - understanding guest-host interactions

⇒ **design of materials with targeted properties, for instance stronger binding energies of H₂**

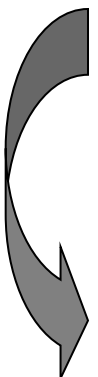
Motivation

calculation of the INS **spectra**

It is essential to have:

i) quantitative description of the **molecule-system potential**

ii) the **methodology** for accurate calculation of the various **spectroscopic observable**



a computer code for **coupled quantum** calculations of the **translational-rotational** energy levels and wave functions of a polyatomic molecule which is confined in (or bounded to) a much heavier entity

Coupled translational rotational problem

5D T-R Hamiltonian:

$$H = -\frac{\hbar}{2m} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) + B\mathbf{j}^2 + V(x, y, z, \theta, \phi)$$

Basis in the angular coordinates – modified spherical harmonics

$$|jm\rangle = \bar{Y}_{jm}(\mathbf{\Omega}) = (-1)^m P_{j,m}(\theta) F_m(\phi) \quad F_m(\phi) = \begin{cases} \pi^{-1/2} \cos(m\phi), & m > 0, \\ (2\pi)^{-1/2}, & m = 0, \\ \pi^{-1/2} \sin(m\phi), & m < 0. \end{cases}$$

I. Matanović et al., J Chem. Phys. 131, 224308 (2009)

Coupled translational rotational problem

5D T-R Hamiltonian:

$$H = -\frac{\hbar}{2m} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) + B\mathbf{j}^2 + V(x, y, z, \theta, \phi)$$

Basis in the x, y, z coordinates – contraction scheme

$$|\Phi_t^{xyz}\rangle = \sum_{q(\alpha\beta\gamma)=1}^{N_{xyz}} {}^{3D}C_{q(\alpha\beta\gamma),t}^{xyz} |X_\alpha\rangle |Y_\beta\rangle |Z_\gamma\rangle,$$

$${}^{3D}h^{xyz} |\Phi_t^{xyz}\rangle = {}^{3D}\epsilon_t^{xyz} |\Phi_t^{xyz}\rangle$$

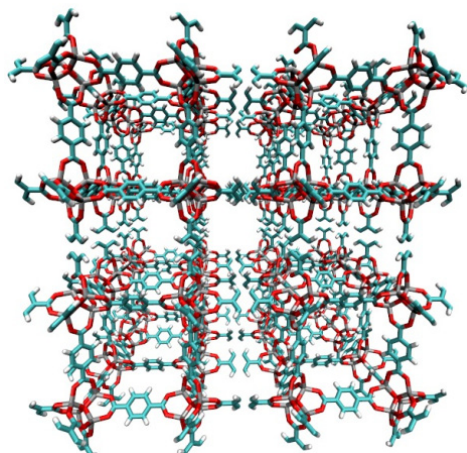
$${}^{3D}h^{xyz} = -\frac{\hbar^2}{2m} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) + \bar{V}(x, y, z) \quad \bar{V}(x, y, z) = \frac{1}{4\pi} \int V(x, y, z, \Omega) d\Omega$$

I. Matanović et al., J Chem. Phys. 131, 224308 (2009)

MOF-5: potential

- analytical form

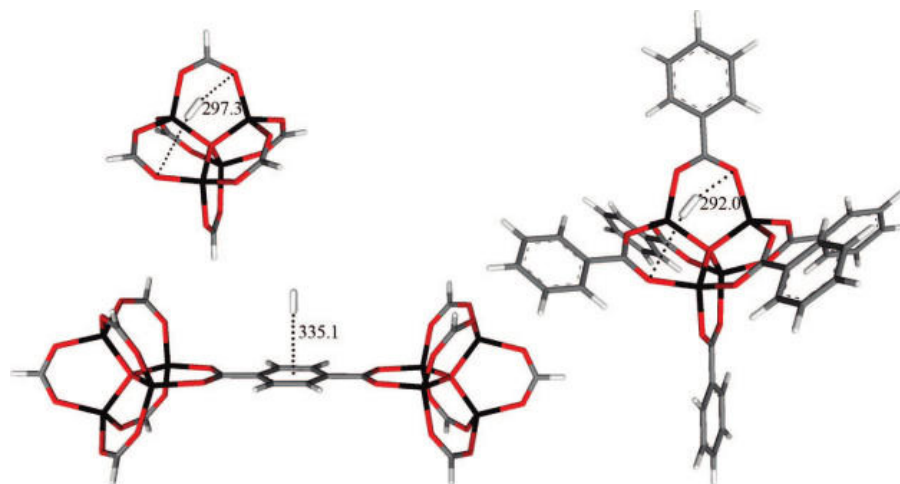
$$V = V_{ES} + V_{LJ} + V_{pol}$$



J. L. Belof, A. C. Stern and B. Space, J. Phys. Chem. C. **2009**, 113, 9116.

- ab initio

MP2/def2-TZVP level



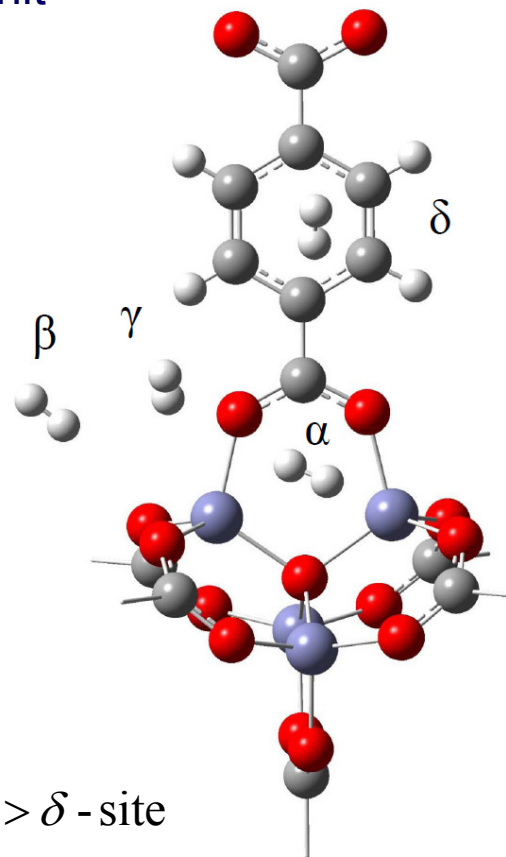
K. Sillar, A. Hofmann, J. Sauer, JACS **2009**, 131, 4143

MOF-5: binding energies

- four binding sites: 4 α -, 4 β -, 12 γ -sites per Zn_4O unit

	analytical PES	ab initio PES
α - site:	-66.6 meV	-82.9 meV
γ - site:	-65.5 meV	-53.9 meV
β - site:	-53.8 meV	-47.7 meV
δ - site:	-37.8 meV	-52.9 meV

exp: α - site \gg γ - site $>$ β - site $>$ δ - site

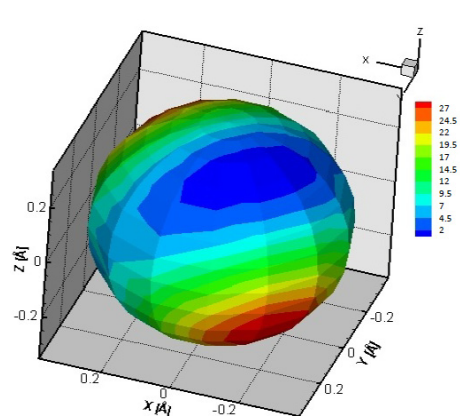


MOF-5: rotational potential

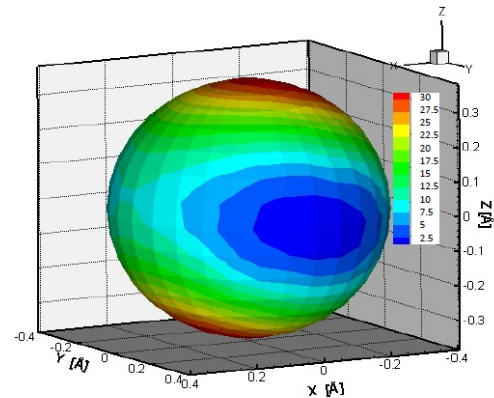
▪ analytical PES

▪ ab initio PES

α - site

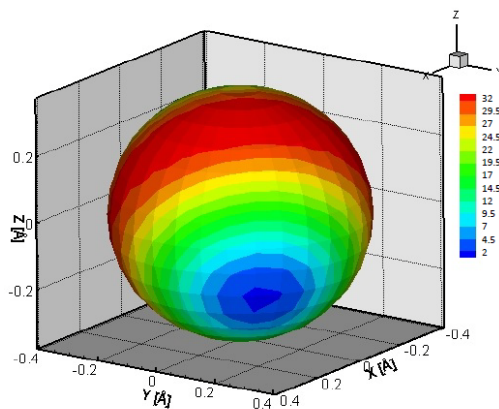


$\text{H}_2\text{-O}_{\text{MOF5}}$ distance: 3.7 Å

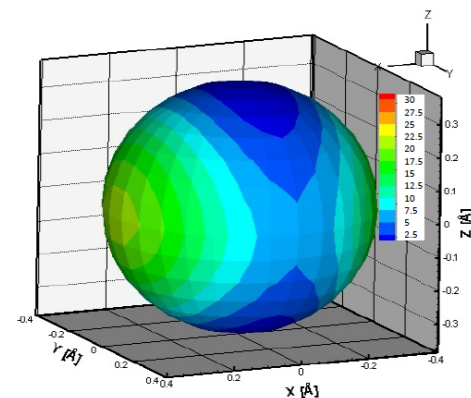


$\text{H}_2\text{-O}_{\text{MOF5}}$ distance: 3.6 Å

γ - site



$\text{H}_2\text{-Zn}_{\text{MOF5}}$ distance: 3.9 Å



$\text{H}_2\text{-Zn}_{\text{MOF5}}$ distance: 4.1 Å

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MOF-5: translational-rotational potential

- analytical PES

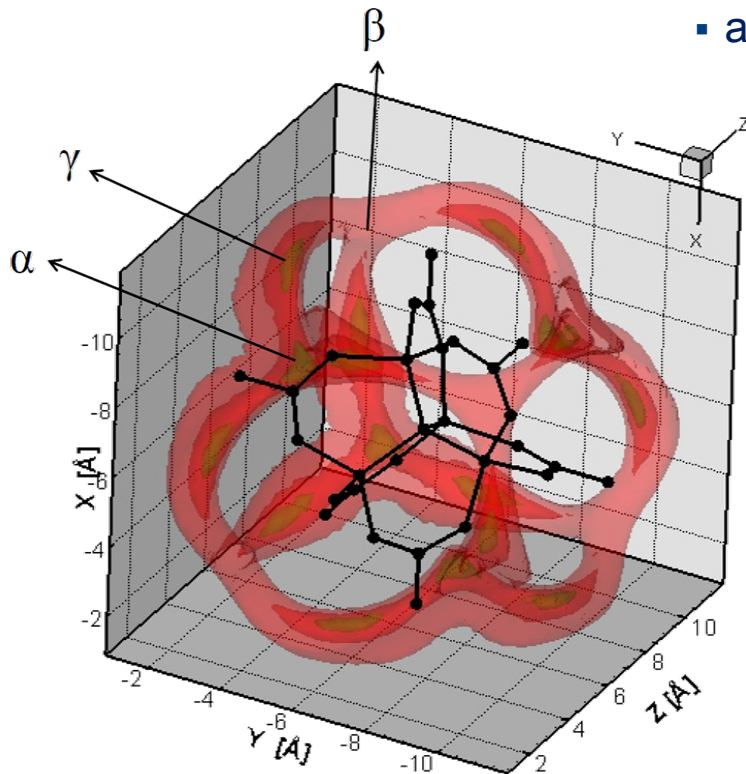


Figure. 3D isosurfaces at -62, -56 and -44 meV for the 5D analytical PES of H₂ in MOF-5

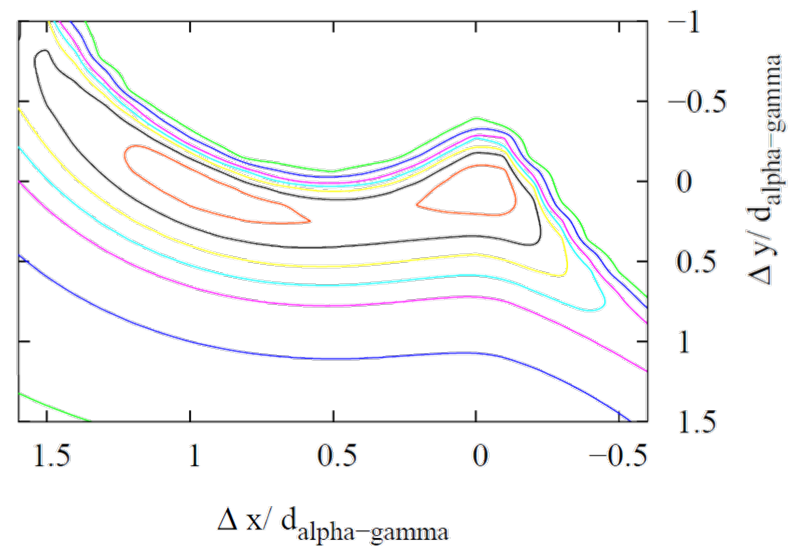
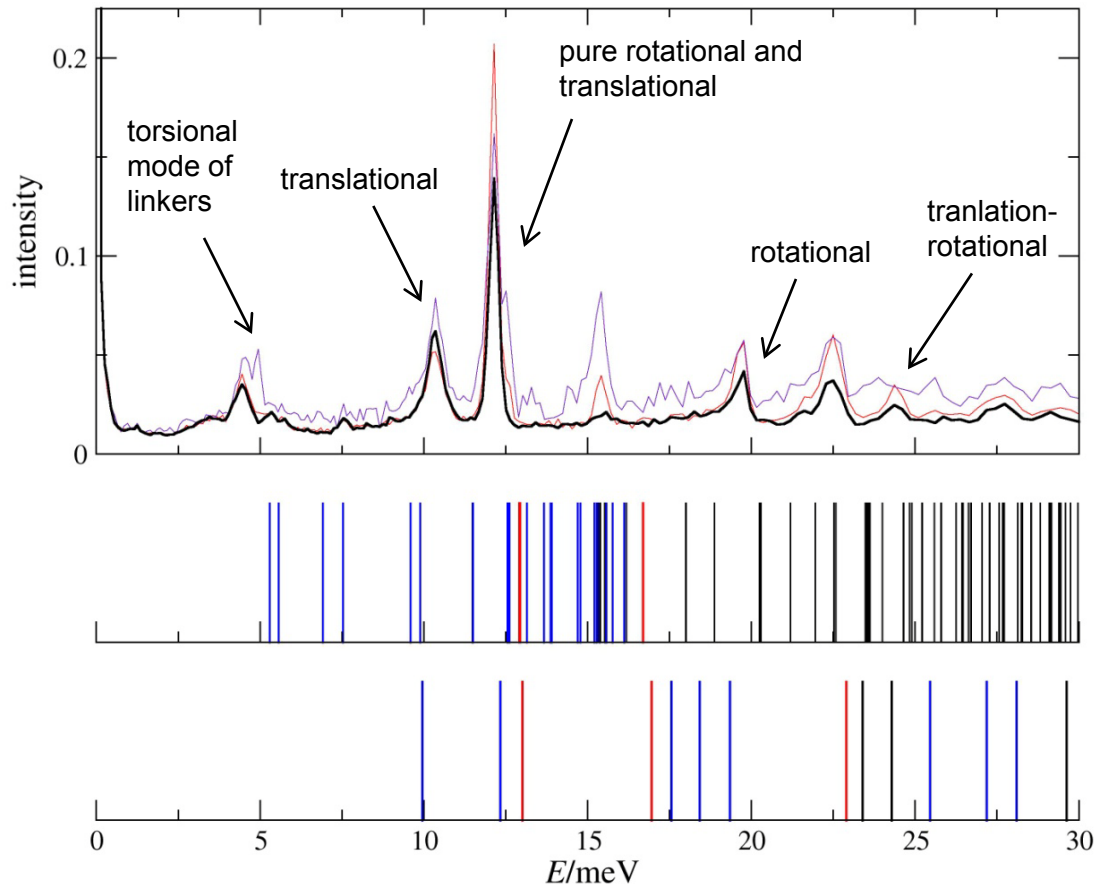


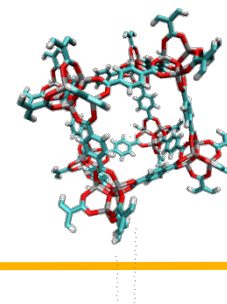
Figure. 2D cut through the potential connecting α - and one of the γ -sites, isosurfaces shown at every 6 meV starting from -62 meV

INS spectra: Translation-rotational problem



1 H_2 moving in α - and γ - sites

1 H_2 moving in α -site with γ -sites occupied

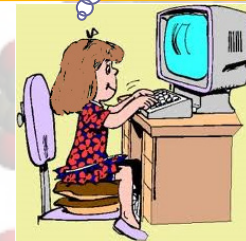
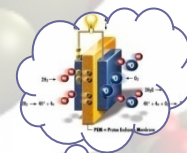


Conclusions

- small barrier between α - and three surrounding γ -sites in MOF-5 on analytical PES by Belof et al.
low-lying translationally excited states extensively delocalized
- comparison with INS spectra implies that the actual degree of localization in the α -site is greater than indicated by the PES
- INS spectra assigned, intensities needed for more extensive assignment – M. Xu et al Phys. Rev. B 84, 195445(2011)
- PESs that accounts for bulk properties (adsorption isotherms) might not correctly describe the interactions with the host on the molecular level – further improvements needed to obtain spectroscopic observables

Acknowledgements

Thank you for your attention



\$\$\$ LANL LDRD program for postdoctoral fellowship, U.S.
Department of Energy, Energy Efficiency and Renewable Energy
for financial support

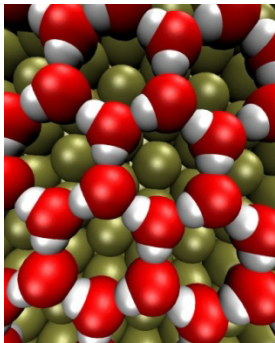
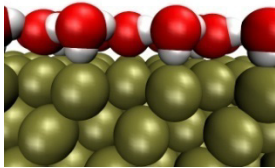
National Energy Research Scientific Computer Center, Pacific
Northwest National Laboratory Advanced Computing Center and
Center for Nanophase Materials Science

Neil Henson & Fernando Garzon
Juergen Eckert & Tony Burrell
C. Taylor and J. Rossmeisl

Different states of the metal surface

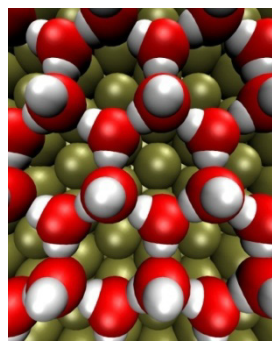
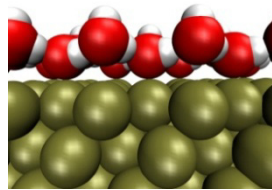
water layer 1

2/3 coverage



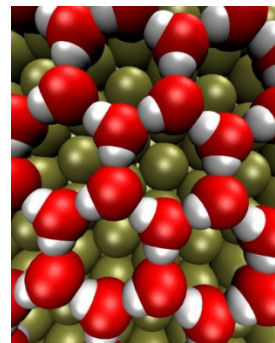
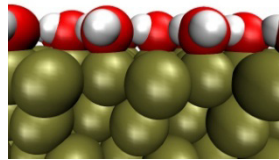
water layer 2

2/3 coverage



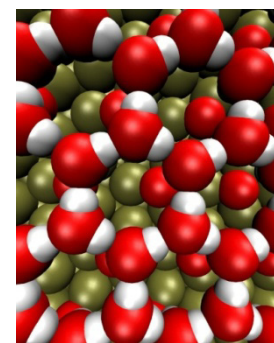
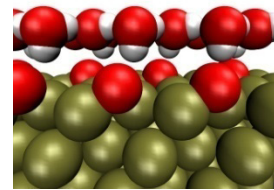
OH + water

1/3 coverage



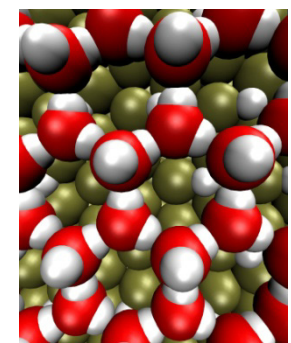
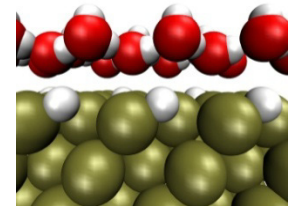
O + water

1/3 coverage



H + water

1/3 coverage



translation- rotation problem

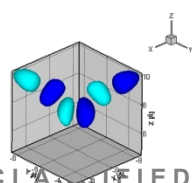
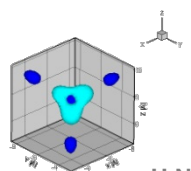
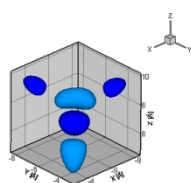
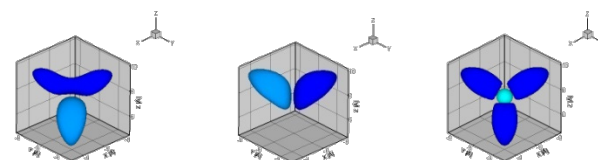
▪ rotational problem in separate wells

▪ translation - rotational problem
(ZPE=218 cm⁻¹ / 2.6 kJ mol⁻¹)

<i>n</i>	alpha /meV	gamma /meV
0	0.0	0.0
1	10.8	7.5
2	13.3	20.2
3	22.6	21.1
4	40.1	42.0
5	40.1	42.4
6	46.8	43.2
7	48.6	52.3
8	51.9	52.3

<i>n</i>	ΔE / meV	type of excitation
0	0.0	
1	5.3 (2)	translational
3	5.6	translational
4	6.9 (2)	translational
6	7.5	translational
7	9.6 (2)	translational
9	9.9	translational
10	11.5(2)	translational
11	12.5 (3)	translational
16	12.91	rotational, <i>j</i> =1
17	12.94	rotational, <i>j</i> =1
35	16.7	rotational, <i>j</i> =1

lower three translational excitations



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